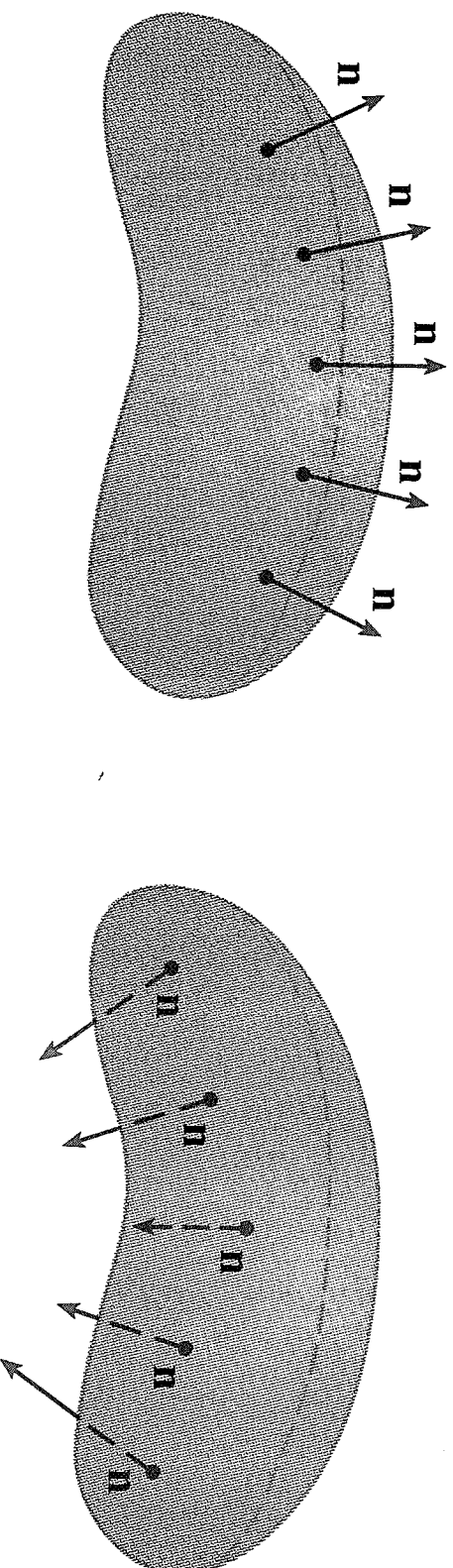


at the same point  $P$  without ever having crossed an edge. (If you have constructed a Möbius strip, try drawing a pencil line down the middle.) Therefore, a Möbius strip really has only one side. You can graph the Möbius strip using the parametric equations in Exercise 30 in Section 16.6.

From now on we consider only orientable (two-sided) surfaces. We start with a surface  $S$  that has a tangent plane at every point  $(x, y, z)$  on  $S$  (except at any boundary points). There are two unit normal vectors  $\mathbf{n}_1$  and  $\mathbf{n}_2 = -\mathbf{n}_1$  at  $(x, y, z)$ . (See Figure 7.) If it is possible to choose a unit normal vector  $\mathbf{n}$  at every such point  $(x, y, z)$  so that  $\mathbf{n}$  varies continuously over  $S$ , then  $S$  is called an **oriented surface** and the given choice of  $\mathbf{n}$  provides  $S$  with an **orientation**. There are two possible orientations for any orientable surface (see Figure 8).



For a surface  $z = g(x, y)$  given as the graph of  $g$ , we use Equation 16.6.7 and see that the induced orientation is given by the unit normal vector

FIGURE 8